

# A COURSE IN LARGE SAMPLE THEORY

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## MAIN ERRATA

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Page 4, line -4. Delete “ $i$ ”, the first character.

Page 6, line 15.  $\mathbf{X}_0$  should be  $\mathbf{x}_0$ .

Line 17.  $F$  should not be bold face.

Page 12, last line. Write  $EX_n^2 \rightarrow EX^2 < \infty$ .

Page 25, line 10.  $X$  should be  $H$ .

Page 26, line -6. Second bold face zero should be  $\mathbf{0}^T$ .

Page 41, line 12.  $=$  should be  $\leq$ .

Page 47, line 7.  $x_1^2$  should be  $\chi_1^2$ .

Page 48, line 5. Should be  $\gamma_n = \sqrt{n}\mu/\sigma$ .

Page 49, Exercise 3(a). Assume  $\mu \neq 0$ . What if  $\mu = 0$ ?

Page 50, line 8.  $x_x^2$  should be  $s_x^2$ .

Page 51, line -7. “6.111...” should be “6”.

Page 71, line -13.  $> \epsilon$  should be  $< \epsilon$ .

Page 72, line 11.  $s/n \rightarrow 1/(k+m)$ , and  $\mathcal{N}(0, \text{Var}(S_k)/(k+m))$ .

Line 17.  $\text{Var}(S_k)/(k+m) \rightarrow \sigma^2$ .

Page 76, line 18. “variance” should be “standard deviation”.

Line 22: “like” should be “likely”.

Page 78, line 7.  $\sigma_2^2$  should be  $\sigma_z^2$ .

Page 79, lines -8 and -3. [ should be [, and ] should be ].

Page 81, line 5 to 6. “ $(n-N)$ ” should be “ $(N-n)$ ”.

Page 82, line -6. Change “is bounded” to “is bounded below by 1”.

Page 84. The second displayed equation should be changed to

$$\frac{S_N - ES_N}{\sqrt{\text{Var}(S_N)}} = \frac{\sqrt{n}(n^{-1}S_N - \bar{z}_N)}{\sqrt{\sigma_z^2(1 - (n/N))}} \xrightarrow{\mathcal{L}} \mathcal{N}(0, 1)$$

Below this expression, add “We may estimate  $\sigma_z^2$  by  $s_z^2$ , the variance of the observed values.”

Page 84, lines -13 and -21.  $s_z^2$  should be  $\sigma_z^2$ .

Page 99, line -1.  $1/2 \log 4\pi$  should be  $(1/2) \log 4\pi$ .

Page 108, line -4. “A real-valued function” should be “An extended real-valued function”.

Page 109, line -8. The proof must be changed because  $\mu(\theta)$  could be  $-\infty$ .  
Lines -1 and -3, and page 110, lines 1 to 4: Each  $X_j$  should be  $X_i$  and each summation should be over  $i$  from 1 to  $n$ .

Page 112, line -6. “may be” should be “may not be”.

Page 127, line -6.  $f(x|\alpha) = \exp\{$  (delete the  $\alpha$ ).  
Line -4.  $\theta(\alpha)$  should be  $g(\alpha)$ .

Page 129, line -11.  $\hat{\theta}^2$  should be  $\tilde{\theta}^2$ .

Page 135 and following.  $\dot{\ell}$  has been defined as a row vector, so here and often in the following  $\dot{\ell}$  should be replaced by  $\dot{\ell}^T$ .

Page 137, line -3.  $\Gamma-$  should be digamma.

Page 155 line 3. This should be written

$$\chi_N^2 = \frac{(n_1 - n(\frac{1}{3} - \theta))^2}{n_1} + \frac{(n_2 - n(\frac{2}{3} - \theta))^2}{n_2} + \frac{(n_3 - 2n\theta)^2}{n_3}.$$

Page 160, line -9. This display should read

$$\|\Pi Z_n - A(\theta_n^*)\|^2 \leq (d_n + \epsilon_n)^2 - (d_n - \epsilon_n)^2 = 4d_n\epsilon_n,$$

Pages 159-161. Unfortunately,  $\Pi$  is used in two different senses. One way to correct this error is to state, after the proof of Corollary 2, that in the rest of the chapter we translate  $A(\theta_0)$  to the origin. (Then the two  $\Pi$ 's are the same.)

Another way is as follows. Before Lemma 2, add: Let  $\phi(z)$  be the projection of  $z$  onto the tangent space at  $A(\theta_0)$ . Then  $\phi(z)$  is the affine transformation

$$\phi(z) = A(\theta_0) + \Pi(z - A(\theta_0)).$$

Then, in Lemma 2 and its proof, replace everywhere  $\Pi Z_n$  by  $\phi(Z_n)$  and  $\Pi A(\theta_n^*)$  by  $\phi(A(\theta_n^*))$ . In addition the second display on page 161 may be written

$$\sqrt{n}(A(\theta_n^*) - A(\theta_0)) \sim \sqrt{n}(\phi(Z_n) - A(\theta_0)) = \sqrt{n}\Pi(Z_n - A(\theta_0)),$$

and in the beginning of the proof of Theorem 24, one may replace “From Lemma 2 of Section 23,” by “From the proof of Theorem 23,”.

Page 172, line 7.  $\mathcal{B}(1, \beta/(\alpha + \beta))$  should be  $\mathcal{B}(1, \alpha/(\alpha + \beta))$ .  
Lines -13 and -12.  $a$  should be  $\alpha$ , twice.

Page 179, lines -10 and -9. Factor of  $c$  omitted.

Page 194, line 10.  $\chi_{c-1}^2$  should be  $\chi_r^2$ .

Page 215, line 7.  $K(X)$  should be  $\exp\{K(X)\}$ .

Line 10.  $\phi(x, \theta, X)$  should be  $\phi(x, \theta, \rho)$ .

Line -11. The formula should read

$$L(\theta) = \left(\frac{2}{\theta}\right)^k \left(\prod_{i \leq k} X_{(i)}\right) \cdot \left(\frac{2}{1-\theta}\right)^{n-k} \left(\prod_{i > k} (1 - X_{(i)})\right).$$

Page 221. There is no Problem #8. Use Additional Exercise Section 19, #1.

Page 228, line 3.  $\mu$  and  $\sigma$  should be  $\alpha$  and  $\beta$  respectively.

Page 229, line 11.  $\phi(\pi(\theta))$  should be  $\dot{\phi}(\pi(\theta))$ .

Page 234, line 6.  $n_{..jk}$  should be  $n_{..k}$ .

## MINOR ERRATA

last update: June 2008

Page viii, line 10. Delete the comma.

Page 5, line 7. Comma between  $n$  and  $X_n$ .  
Next line, remove absolute value signs around  $Y$ .

Page 8, lines 12 and 13, and page 9, lines -9, -8 and -6. The  $\epsilon$ 's should be  $\in$ .

Page 11, lines 22-23. Superposition of indices.  
line -8, use  $E|X_n - X|^2$  instead of  $E(X_n - X)^2$ .

Page 16, line -3. Need closing curly brace for exp.

Page 20, line 4.  $\dot{g}(x)$  should be  $\dot{\mathbf{g}}(\mathbf{x})$ .

Page 21, line 1. Change  $t'$  to  $t^T$ .  
Line 3. bold face 0.  
Line -11. bold face epsilon.

Page 23, line -13. Wrong symbol for epsilon.

Page 26, line -6.  $\mu$  should be bold face  $\mu$ .

Page 27, line 15. "ad" should be "and".

Page 34, line 2. Both  $X$  should be bold face.  
Line 14: "3" should be "3."

Page 45, line 4. 0 should be bold face 0.

Page 63, line -12.  $\Sigma$  should be bold face  $\Sigma$ .

Page 64, line -3. The first  $\mathbf{Y}$  should be  $\mathbf{Y}^T$ .

Page 72, line -4.  $J$  should be  $j$ .

Page 73, line -12. First summation should be over  $i$ .  
Line -6. "ad" should be "and".

Page 75, first display. The sum should be over  $j$ .

Page 77, line -3. Lindeberg (sp.)

Page 91, line 4. Bracket in subscript of first  $X$  should be parenthesis.

Page 95, line -11. "extremal" should be "extreme value".

Page 97, line 12.  $n \rightarrow \infty$  should be below lim.

Page 103, line 7.  $Z_{1,N}$  should be  $Z_{1,n}$ .

Page 109, line 6. The  $U$  should be slanted.

Page 112, line -12. Bold face  $L$  should be plain face.

Page 113, line 13. “convex” should be “concave”.

Line 17. Integration should be over  $S_0$ .

Page 115, line -6. Parthasarathy (sp.).

Page 119, line 4. The partial derivative should be over bold face  $\theta$ .

Line -4. Add a space after the word “of”.

Page 120, line 7.  $f(x\theta)$  should be  $f(x|\theta)$ .

Page 122, line -5. In  $\mathcal{N}(0, \mathcal{I}(\theta_0)^{-1})$  the 0 should be bold face.

Line -3. (3) should be (2).

Page 126, display (1).  $f(X, \theta)$  should be  $f(X|\theta)$ .

Pages 126 to 128. Too much space between  $\hat{\theta}$  and  $(X)$ , (eight times).

Page 127, lines 9-10. “coefficient”.

Line -14. “if and only if”.

Page 130, line -11. A  $\theta$  should be made bold face.

Page 131 lines -10 and -11. Delete the equal sign and the digamma sign.

Page 132, line 1. “Checking” should be “Check”.

Page 145, last 5 lines.  $\theta_0$  should be bold face (3 times).

Page 147, line 6. The second [ should be ].

Page 148, line -3. The second [ should be ].

Page 155, lines -7 and -8. The sum is over  $j$ , so  $i$  should be  $j$ , and the subscript 1 should be  $j$ .

Page 157, line -2.  $(a - z_i)$  should be  $(a_i - z_i)$ .

Page 175, line -3. Schwarz (sp.).

Page 180, line -2. Missing right parenthesis at end of line.

Page 201, line 13.  $(m/N \rightarrow r)$  should be  $(m/N - r)$ .

Page 210, line 12.  $N$  should be  $n$ .

Page 216, line 7. “and” should be “are”.

Line 10. Delete “(c)”. The answer to part (c) seems to have been omitted.

Page 218, line -3. The = should be >.

Page 224, line 4. Remove the last ).

Page 233, last 4 lines and page 234 first 8 lines. The double dot subscripts are hard to read.

Page 239. Cauchy (sp.).

Page 244. Schwarz (sp.).